Chapter Title	Prediction of Structures and Ir	nteractions from Genome Information
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Abstract	Predicting three dimensional residue-residue contacts from evolutionary information in protein sequences was attempted already in the early 1990s. However, contact prediction accuracies of methods evaluated in CASP experiments before CASP11 remained quite low, typically with <20% true positives. Recently, contact prediction has been significantly improved to the level that an accurate three dimensional model of a large protein can be generated on the basis of predicted contacts. This improvement was attained by disentangling direct from indirect correlations in amino acid covariations or cosubstitutions between sites in protein evolution. Here, we review statistical methods for extracting causative correlations and various approaches to describe protein structure, complex, and flexibility based on predicted contacts.	
Keywords (separated by "-")	Contact prediction - Direct co Amino acid cosubstitution - I model - Inverse Potts model machine - Deep neural netwo	oupling - Amino acid covariation - Partial correlation - Maximum entropy - Markov random field - Boltzmann ork

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Chapter 9 Prediction of Structures and Interactions from Genome Information

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Abstract Predicting three dimensional residue-residue contacts from evolutionary information in protein sequences was attempted already in the early 1990s. 6 However, contact prediction accuracies of methods evaluated in CASP experiments 7 before CASP11 remained quite low, typically with <20% true positives. Recently, 8 contact prediction has been significantly improved to the level that an accurate three 9 dimensional model of a large protein can be generated on the basis of predicted 10 contacts. This improvement was attained by disentangling direct from indirect 11 correlations in amino acid covariations or cosubstitutions between sites in protein 12 evolution. Here, we review statistical methods for extracting causative correlations 13 and various approaches to describe protein structure, complex, and flexibility based 14 on predicted contacts. 15

KeywordsContact prediction · Direct coupling · Amino acid covariation ·16Amino acid cosubstitution · Partial correlation · Maximum entropy model ·17Inverse Potts model · Markov random field · Boltzmann machine · Deep neural18network19

9.1 Introduction

The evolutionary history of protein sequences is a valuable source of information 21 in many fields of science not only in evolutionary biology but even to understand 22 protein structures. Residue-residue interactions that fold a protein into a unique 23 three-dimensional (3D) structure and make it play a specific function impose struc- 24 tural and functional constraints in varying degrees on each amino acid. Selective 25 constraints on amino acids are recorded in amino acid orders in homologous protein 26 sequences and also in the evolutionary trace of amino acid substitutions. Negative 27

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H. Nakamura et al. (eds.), *Integrative Structural Biology with Hybrid Methods*, Advances in Experimental Medicine and Biology 1105, https://doi.org/10.1007/978-981-13-2200-6_9



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effects caused by mutations at one site must be compensated by successive muta-28 tions at other sites (Yanovsky et al. 1964; Fitch and Markowitz 1970; Maisnier-Patin 29 and Andersson 2004), causing covariations/cosubstitutions/coevolution between 30 sites (Tufféry and Darlu 2000; Fleishman et al. 2004; Dutheil et al. 2005; Dutheil 31 and Galtier 2007), otherwise most negative mutants will be eliminated from a 32 gene pool and never reach fixation in population. Such structural and functional 33 constraints arise from interactions between sites mostly in close spatial proximity. 34 Thus, it has been suggested and also shown that the types of amino acids (Lapedes 35 et al. 1999, 2002, 2012; Russ et al. 2005; Skerker et al. 2008; Burger and van 36 Nimwegen 2008; Weigt et al. 2009; Halabi et al. 2009; Burger and van Nimwegen 37 2010; Morcos et al. 2011; Marks et al. 2011) and amino acid substitutions (Altschuh 38 et al. 1988; Göbel et al. 1994; Shindyalov et al. 1994; Pollock and Taylor 1997; 39 Pollock et al. 1999; Atchley et al. 2000; Fariselli et al. 2001; Fodor and Aldrich 40 2004; Fleishman et al. 2004; Dutheil et al. 2005; Martin et al. 2005; Fares and 41 Travers 2006; Doron-Faigenboim and Pupko 2007; Dutheil and Galtier 2007; Dunn 42 et al. 2008; Poon et al. 2008; Dutheil 2012; Gulyás-Kovács 2012) are correlated 43 between sites that are close in a protein 3D structure. However, until CASP11, 44 contact prediction accuracy remained quite low, typically with $\leq 20\%$ true positives 45 for top-L/5 long-range contacts in free modeling targets (Kosciolek and Jones 46 2016); L denotes protein length. Recently contact prediction has been significantly 47 improved to the level that an accurate three dimensional model of a large protein 48 ($\simeq 250$ residues) can be generated on the basis of predicted contacts (Moult et al. 49 2016). These improvements were attained primarily by disentangling direct from $_{50}$ indirect correlations in amino acid covariations or cosubstitutions between sites in 51 protein evolution, and secondarily by reducing phylogenetic biases in a multiple 52 sequence alignment (MSA) or removing them on the basis of a phylogenetic tree; 53 see Fig. 9.1. 54

Here, we review statistical methods for extracting causative correlations in amino ⁵⁵ acid covariations/cosubstitutions between sites, and various approaches to describe ⁵⁶ protein structure, complex and flexibility based on predicted contacts. Mathematical ⁵⁷ formulation of each statistical method is concisely described in the unified manner ⁵⁸ in an appendix, the full version of which will be found in the article (Miyazawa ⁵⁹ 2017a) submitted to arXiv. ⁶⁰

9.2 Statistical Methods to Extract Causative Interactions Between Sites

The primary task to develop a robust method toward contact prediction is to 63 detect causative correlations, which reflect evolutionary constraints, in amino acid 64 covariations between sites in a multiple sequence alignment (MSA) or in amino acid 65 cosubstitutions between sites in branches of a phylogenetic tree; see Table 9.1. The 66 former was called direct coupling analysis (DCA) (Morcos et al. 2011). 67

Category		
Method name	Method/algorithm	t3.1
(A) Direct coupling analysis of amin	no acid covariations between sites in a MSA	
Boltzmann machine	Markov chain Monte Carlo to calculate marginal probabilities and gradient descent to estimate fields and couplings	t3.2
CMI (Lapedes et al. 2012)	Boltzmann machine to estimate conditional mutual information	t3.3
mpDCA (Weigt et al. 2009)	Message-passing algorithm to estimate marginal probabilities and gradient descent to estimate fields and couplings	t3.4
mfDCA (Morcos et al. 2011; Marks et al. 2011)	Mean field approximation to estimate the partition function	t3.5
PSICOV (Jones et al. 2012)	Graphical lasso (Gaussian approximation with an exponential prior) with a shrinkage method for a covariance matrix	t3.6
GaussDCA (Baldassi et al. 2014)	A multivariate Gaussian model with a normal- inverse-Wishart prior	t3.7
plmDCA (Ekeberg et al. 2013, 2014)	Pseudo-likelihood maximization with Gaussian priors (ℓ_2 regularizers)	t3.8
GREMLIN (Balakrishnan et al. 2011; Kamisetty et al. 2013)	Pseudo-likelihood maximization with ℓ_1 regularization terms (Balakrishnan et al. 2011) or with Gaussian priors (Kamisetty et al. 2013) which depend on site pair	t3.9
ACE (Cocco and Monasson 2011, 2012; Barton et al. 2016)	Adaptive cluster expansion of cross-entropy with Gaussian priors	t3.1
Persistent VI & Fadeout	Variational inference with sparsity-inducing prior, horseshoe (Ingraham and Marks 2016)	t3.1 ⁻
Sutto et al. (2015)	Boltzmann machine with ℓ_2 regularization terms	t3.1
DI (Taylor and Sadowski 2011)	Partial correlation of normalized mutual informations between sites	t3.1
(B) Partial correlation analysis of an	nino acid cosubstitutions between sites in a phylogenetic tree	
pcSV (Miyazawa 2013)	Partial correlation coefficients of coevolutionary sub- stitutions between sites within branches in a phyloge- netic tree	t3.14

 Table 9.1
 Statistical methods for disentangling direct from indirect correlations between sites

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9.2.1 Direct Coupling Analysis for Amino Acid Covariations Between Sites in a Multiple Sequence Alignment

The direct coupling analysis is based on the maximum entropy model for the 70 distribution of protein sequences, which satisfies the observed statistics in a MSA. 71

9.2.1.1 Maximum Entropy Model for the Distribution of Protein Sequences

Let us consider probability distributions $P(\sigma)$ of amino acid sequences, $\sigma \equiv 74$ $(\bigcirc_1, \ldots, \bigcirc_L)^T$ with $\bigcirc_i \in \{\text{amino acids, deletion}\}$, single-site and two-site marginal 75 probabilities of which are equal to a given frequency $P_i(a_k)$ of amino acid a_k at 76 each site *i* and a given frequency $P_{ij}(a_k, a_l)$ of amino acid pair (a_k, a_l) for site pair 77 (i, j), respectively. 78

$$P(\mathbf{\hat{g}}_i = a_k) \equiv \sum_{\mathbf{\sigma}} P(\mathbf{\sigma}) \delta_{\mathbf{\hat{g}}_i a_k} = P_i(a_k)$$
(9.1)

$$P(\mathbf{\hat{g}}_{i} = a_{k}, \mathbf{\hat{g}}_{j} = a_{l}) \equiv \sum_{\sigma} P(\sigma) \delta_{\mathbf{\hat{g}}_{i}a_{k}} \delta_{\mathbf{\hat{g}}_{j}a_{l}} = P_{ij}(a_{k}, a_{l})$$
(9.2)

where $a_k \in \{\text{amino acids, deletion}\}, k = 1, ..., q, q \equiv |\{\text{amino acids, deletion}\}| = 79$ 21, i, j = 1, ..., L, and $\delta_{\beta_i a_k}$ is the Kronecker delta. The distribution P_{ME} with the 80 maximum entropy is 81

$$P_{\text{ME}}(\boldsymbol{\sigma}|h, J)$$

$$= \arg \max_{P(\boldsymbol{\sigma})} [-\sum_{\boldsymbol{\sigma}} P(\boldsymbol{\sigma}) \log P(\boldsymbol{\sigma}) + \lambda (\sum_{\boldsymbol{\sigma}} P(\boldsymbol{\sigma}) - 1) \\ + \sum_{i} [h_{i}(a_{k})(\sum_{\boldsymbol{\sigma}} P(\boldsymbol{\sigma}) \delta_{\boldsymbol{\theta}_{i}a_{k}} - P_{i}(a_{k}))] \\ + \sum_{i} \sum_{j>i} [J_{ij}(a_{k}, a_{l})(\sum_{\boldsymbol{\sigma}} P(\boldsymbol{\sigma}) \delta_{\boldsymbol{\theta}_{i}a_{k}} \delta_{\boldsymbol{\theta}_{j}a_{l}} - P_{ij}(a_{k}, a_{l}))]] = \frac{1}{Z} e^{-H_{\text{Potts}}(\boldsymbol{\sigma}|h, J)}$$

$$(9.3)$$

where λ , $h_i(a_k)$, and $J_{ij}(a_k, a_l)$ are Lagrange multipliers, and a Hamiltonian H_{Potts} , 82 which is called that of the Potts model for q > 2 (or the Ising model for q = 2), and 83 a partition function Z are defined as 84

$$-H_{\text{Potts}}(\boldsymbol{\sigma}|h,J) = \sum_{i} h_{i}(\boldsymbol{\sigma}_{i}) + \sum_{i < j} J_{ij}(\boldsymbol{\sigma}_{i},\boldsymbol{\sigma}_{j}), \quad Z = \sum_{\boldsymbol{\sigma}} e^{-H_{\text{Potts}}(\boldsymbol{\sigma}|h,J)}$$
(9.5)

where $h_i(a_k)$ and $J_{ii}(a_k, a_l)$ are interaction potentials called fields and couplings. 85

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(9.4)

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Although pairwise frequencies $P_{ij}(a_k, a_l)$ reflect not only direct but indirect ⁸⁶ correlations in amino acid covariations between sites, couplings $J_{ij}(a_k, a_l)$ reflect ⁸⁷ causative correlations only. Thus, it is essential to estimate fields and couplings from ⁸⁸ marginal probabilities. This model is called the inverse Potts model. ⁸⁹

9.2.1.2 Log-Likelihood and Log-Posterior-Probability

Log-posterior-probability and log-likelihood for the Potts model are

$$\log P_{\text{post}}(h, J|\{\sigma\}) \propto \ell_{\text{Potts}}(\{P_i\}, \{P_{ij}\}|h, J) + \log P_0(h, J)$$
(9.6)
$$\ell_{\text{Potts}}(\{P_i\}, \{P_{ij}\}|h, J) = B \sum_{\sigma} P_{\text{obs}}(\sigma) \log P_{\text{ME}}(\sigma|h, J)$$
(9.7)

where $P_{obs} \equiv \sum_{\tau=1}^{B} \delta_{\sigma\sigma\tau}/B$ is the observed distribution of σ specified with $_{92} \{P_i(a_k)\}$ and $\{P_{ij}(a_k, a_l)\}$, and *B* is the number of instances; sequences σ^{τ} are $_{93}$ assumed here to be independently and identically distributed samples in sequence $_{94}$ space. $P_0(h, J)$ is a prior probability of (h, J).

Let us define cross entropy (Cocco and Monasson 2012) as the negative logposterior-probability per instance. 97

$$S_{0}(h, J|\{P_{i}\}, \{P_{ij}\}) \propto -(\log P_{\text{post}}(h, J|\{\sigma\}))/B$$

$$\equiv S_{\text{Potts}}(h, J|\{P_{i}\}, \{P_{ij}\}) + R(h, J)$$
(9.8)

where the cross entropy S_{Potts} , which is the negative log-likelihood per instance for 98 the Potts model, and the negative log-prior per instance *R* are defined as follows. 99

$$S_{\text{Potts}}(h, J|\{P_i\}, \{P_{ij}\}) \equiv -\ell_{\text{Potts}}(\{P_i\}, \{P_{ij}\}|h, J)/B$$
(9.9)

$$= \log Z(h, J) - \sum_{i} \sum_{k} h_{i}(a_{k}) P_{i}(a_{k}) - \sum_{i} \sum_{k} \sum_{j>i} \sum_{l} J_{ij}(a_{k}, a_{l}) P_{ij}(a_{k}, a_{l})$$
(9.10)
(9.10)

$$R(h, J) \equiv -\log(P_0(h, J))/B \tag{9.11}$$

The maximum likelihood estimates of *h* and *J*, which minimize the cross entropy 101 with R = 0, satisfy the following equations. 102

$$\frac{\partial \log Z(h,J)}{\partial h_i(a_k)} = P_i(a_k), \quad \frac{\partial \log Z(h,J)}{\partial J_{ij}(a_k,a_l)} = P_{ij}(a_k,a_l) \tag{9.12}$$

It is, however, hardly tractable to computationally evaluate the partition function 103Z(h, J) for any reasonable system size as a function of h and J. Thus, approximate 104 maximization of the log-likelihood or minimization of the cross entropy is needed 105 to estimate h and J.

The minimum of the cross entropy with R = 0 for the Potts model is just the 107 Legendre transform of log Z(h, J) from (h, J) to $(\{P_i\}, \{P_{ij}\})$, (Eq. 9.10), and is 108 equal to the entropy of the Potts model satisfying Eqs. 9.1 and 9.2; 109

$$S_{\text{Potts}}(\{P_i\}, \{P_{ij}\}) \equiv \min_{h, J} S_{\text{Potts}}(h, J | \{P_i\}, \{P_{ij}\}) = \sum_{\sigma} -P(\sigma) \log P(\sigma) \quad (9.13)$$

The cross entropy $S_{\text{Potts}}(h, J|\{P_i\}, \{P_{ij}\})$ in Eq. 9.10 is invariant under the a certain 110 transformation of fields and couplings, $J_{ij}(a_k, a_l) \rightarrow J_{ij}(a_k, a_l) - J_{ij}^1(a_k) - 111$ $J_{ji}^1(a_l) + J_{ij}^0, h_i(a_k) \rightarrow h_i(a_k) - h_i^0 + \sum_{j \neq i} J_{ij}^1(a_k)$ for any $J_{ij}^1(a_k), J_{ij}^0$ and h_i^0 . This 112 gauge-invariance reduces the number of independent variables in the Potts model to 113 (q-1)L fields and $(q-1)L \times (q-1)L$ couplings. 114

A prior $P_0(h, J)$ yields regularization terms for h and J (Cocco and Monasson 115 2012). If a Gaussian distribution is employed for the prior, then it will yield ℓ_2 norm 116 regularization terms. ℓ_1 norm regularization corresponds to the case of exponential 117 priors. Given marginal probabilities, the estimates of fields and couplings are those 118 minimizing the cross entropy. 119

$$(h, J) = \arg\min_{(h, J)} S_0(h, J | \{P_i\}, \{P_{ij}\}), \ S_0(\{P_i\}, \{P_{ij}\}) \equiv \min_{(h, J)} S_0(h, J | \{P_i\}, \{P_{ij}\})$$
(9.14)

Since $S_0(\{P_i\}, \{P_{ij}\})$ is the Legendre transform of $(\log Z(h, j) + R(h, J))$ from 120 (h, J) to $(\{P_i\}, \{P_{ij}\})$, these optimum *h* and *J* can also be calculated from 121

$$h_i(a_k) = -\frac{\partial S_0(\{P_i\}, \{P_{ij}\})}{\partial P_i(a_k)}, \quad J_{ij}(a_k, a_l) = -\frac{\partial S_0(\{P_i\}, \{P_{ij}\})}{\partial P_{ij}(a_k, a_l)}$$
(9.15)

In most methods for contact prediction, residue pairs are predicted as contacts in 122 the decreasing order of score (S_{ij}) calculated from fields $\{J_{ij}(a_k, a_l)|1 \le k, l < q\}$; 123 see Eq. 9.47. 124

9.2.1.3 Inverse Potts Model

The problem of inferring interactions from observations of instances has been 126 studied as inverse statistical mechanics, particularly inverse Potts model for Eq. 9.4, 127 in the filed of statistical physics, as a Markov random field, Markov network or 128 undirected graphical model in the domain of physics, statistics and information 129 science, and as Boltzmann machine in the field of machine learning.

The maximum-entropy approach to the prediction of residue-residue contacts ¹³¹ toward protein structure prediction from residue covariation patterns was first ¹³² described in 2002 by Lapedes and collaborators (Giraud et al. 1999; Lapedes ¹³³ et al. 1999, 2002, 2012). They estimated conditional mutual information (CMI), ¹³⁴ which was employed as a score for residue-residue contacts, for each site pair by ¹³⁵ Boltzmann leaning with Monte Carlo importance sampling to calculate equilibrium ¹³⁶

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averages and gradient descent to minimize the cross entropy and successfully 137 predicted contacts for 11 small proteins.

Calculating marginal probabilities for given fields and couplings by Monte Carlo 139 simulations in Boltzmann machine is very computationally intensive. To reduce 140 a computational load, the message passing algorithm, which is exact for a tree 141 topology of couplings but approximate for the present model, is employed instead 142 in mpDCA (Weigt et al. 2009). Because even the message passing algorithm is 143 too slow to be applied to a large-scale analysis across many protein families, the 144 mean field approximation is employed in mfDCA (Morcos et al. 2011; Marks et al. 145 2011); $J^{MF} = -C^{-1}$, where $C_{ij}(a_k, a_l) \equiv P_{ij}(a_k, a_l) - P_i(a_k)P_i(a_l)$. In the mean 146 field approximation, a bottleneck in computation is the calculation of the inverse 147 of a covariance matrix *C* that is a $(q - 1)L \times (q - 1)L$ matrix. In the mean 148 field approximation, a prior distribution in Eq. 9.11 is ignored and pseudocount is 149 employed instead of regularization terms to make the covariance matrix invertible. 150

The Gaussian approximation (a continuous multivariate Gaussian model) for the 151 probability distribution of sequences is employed together with an exponential prior 152 (an ℓ_1 regularization term) in PSICOV (Jones et al. 2012), and with a normalinverse-Wishart (NIW) prior, which is a conjugate distribution of the multivariate 154 Gaussian, in GaussDCA (Baldassi et al. 2014). The use of NIW prior has a merit that fields and couplings can be analytically formulated; see Eqs. 9.30 and 9.31. 156

All methods based on the Gaussian approximation employ the analytical formula 157 for couplings, $J \simeq -C^{-1} = -\Theta$, which are essentially as same as the mean field 158 approximation with a difference that the covariance matrix (*C*) or precision matrix 159 (Θ) is differently estimated based on the various priors. The mean field and Gaussian approximations may be appropriate to systems of dense and weak couplings 161 but questionable for sparse and strong couplings that is the characteristic of residueresidue contact networks. Although the mean field and Gaussian approximations 163 successfully predict residue-residue contacts in proteins, it has been shown (Barton 164 et al. 2016; Cocco et al. 2017) that they do not give the accurate estimates of fields 165 and couplings in proteins. 166

A pseudo-likelihood with Gaussian priors (ℓ_2 regularization terms) is maximized 167 to estimate fields and couplings in plmDCA (Ekeberg et al. 2013, 2014) for the 168 Potts model with sparse interactions as well as reducing computational time; see 169 Eq. 9.38 for the symmetric plmDCA and Eq. 9.41 for the asymmetric plmDCA. The 170 asymmetric plmDCA method (Ekeberg et al. 2014) requires less computational time 171 and fits particularly with parallel computing. 172

GREMLIN (Kamisetty et al. 2013) employs together with pseudo-likelihood 173 Gaussian priors that depend on site pair, although its earlier version (Balakrishnan 174 et al. 2011) employed ℓ_1 regularizers, which may be more appropriate to systems of 175 sparse couplings. The ℓ_1 regularizers appear to learn parameters that are closer to 176 their true strength, but the ℓ_2 regularizers appear to be as good as the ℓ_1 regularizers 177 for the task of contact prediction that requires the relative ranking of the interactions 178 and not their actual values (Kamisetty et al. 2013). 179

One of approaches to surpass the pseudo-likelihood approximation for systems 180 of sparse couplings may be the adaptive cluster expansion (ACE) of cross 181

entropy (Cocco and Monasson 2011, 2012; Barton et al. 2016), in which cross 182 entropy is approximately minimized by taking account of only site clusters 183 the incremental entropy (cluster entropy) of which by adding one more site is 184 significant. In this method (Barton et al. 2016), a Boltzmann machine is employed 185 to refine fields and couplings and also to calculate model correlations such as 186 single-site and pairwise amino acid frequencies under given fields and couplings. 187 The results of the Boltzmann machine for both biological and artificial models 188 showed that ACE outperforms plmDCA in recovering single-site marginals (amino 189 acid frequencies at each site) and the distribution of the total dimensionless 190 energies $(H_{Potts}(\sigma))$ (Barton et al. 2016); those models were a lattice protein, 191 trypsin inhibitor, HIV p7 nucleocapsid protein, multi-electrode recording of cortical 192 neurons, and Potts models on Eridös-Rényi random graphs. More importantly ACE 193 could accurately recover the true fields h and couplings J corresponding to Potts 194 states with $P_i(a_k) \ge 0.05$ for Potts models (L = 50) on Eridös-Rényi random 195 graphs (Barton et al. 2016). On the other hand, plmDCA gave accurate estimates 196 of couplings at weak regularization for well sampled single-site probabilities, but 197 less accurate fields. Also, plmDCA yielded less well inferred fields and couplings 198 for single-site and two-site probabilities not well sampled, indicating that not 199 well populated states should be merged. As a result, the distribution of the total 200 energies (Barton et al. 2016) and the distribution of mutations with respect to 201 the consensus sequence were not well reproduced (Cocco et al. 2017). Similarly, 202 the mean field approximation could not reproduce two-site marginals and even 203 single-site marginals (Cocco et al. 2017) and the Gaussian approximation could 204 not well reproduce the distribution of mutations with respect to the consensus 205 sequence (Barton et al. 2016). 206

However, the less reproducibility of couplings does not necessarily indicate 207 the less predictability of residue-residue contacts, probably because in contact 208 prediction the relative ranking of scores (Eq. 9.47) based on couplings is more 209 important than their actual values. ACE with the optimum regularization strength 210 with respect to the reproducibility of fields and couplings showed less accurate 211 contact prediction than plmDCA and mfDCA. For ACE to show comparable 212 performance of contact prediction with plmDCA, regularization strength had to be 213 increased from $\gamma = 2/B = 10^{-3}$ to $\gamma = 1$ for Trypsin inhibitor, making couplings 214 strongly damped and then the generative properties of inferred models lost (Barton 215 et al. 2016) (Table 9.2). 216

9.2.2 Partial Correlation of Amino Acid Cosubstitutions 217 Between Sites at Each Branch of a Phylogenetic Tree 218

In the DCA analyses on residue covariations between sites in a multiple sequence ²¹⁹ alignment (MSA), phylogenetic biases, which are sequence biases due to phyloge- ²²⁰ netic relations between species, in the MSA must be removed as well as indirect ²²¹ 9 Prediction of Structures and Interactions from Genome Information

Name	Methods	URL
EVcouplings (Marks et al. 2011)	mfDCA	http://evfold.org
EVcouplings, plmc (Toth-Petroczy et al. 2016; Weinreb et al. 2016)	mf/plmDCA	https://github.com/debbiemarkslab
DCA (Morcos et al. 2011; Marks et al. 2011)	mfDCA	http://dca.rice.edu/portal/dca/home
GaussDCA (Baldassi et al. 2014)	GaussDCA	http://areeweb.polito.it/ricerca/cmp/code
FreeContact (Kaján et al. 2014)	mfDCA, PSICONV	http://rostlab.org/owiki/index.php/ FreeContact
plmDCA (Ekeberg et al. 2013, 2014)	plmDCA	http://plmdca.csc.kth.se/ https://github.com/pagnani/plmDCA
CCMpred (Seemayer et al. 2014)	plmDCA	Performance-optimized software https://github.com/soedinglab/ccmpred
GREMLIN (Balakrishnan et al. 2011; Kamisetty et al. 2013)	GREMLIN	http://gremlin.bakerlab.org/
ACE (Cocco and Monasson 2011, 2012; Barton et al. 2016)	ACE	https://github.com/johnbarton/ACE
Persistent-vi (Ingraham and Marks 2016)	Persistent VI	https://github.com/debbiemarkslab

 Table 9.2
 Free softwares/servers for the direct coupling analysis

correlations between sites, but instead are reduced by taking weighted averages 222 over homologous sequences in the calculation of single and pairwise frequencies 223 of amino acids. 224

Needless to say, it is supposed that observed patterns of covariation were caused 225 by molecular coevolution between sites. Whatever caused covariations found in the 226 MSA, it has been confirmed that they can be utilized to predict residue pairs in 227 close proximity in a three dimensional structure. Talavera et al. (2015) claimed, 228 however, that covarying substitutions were mostly found on different branches of 229 the phylogenetic tree, indicating that they might or might not be attributable to 230 coevolution. 231

In order to remove phylogenetic biases and also to respond to such a claim above, 232 it is meaningful to study covarying substitutions between sites in a phylogenetic 233 tree-dependent manner. Such an alternative approach was taken to infer coevolving 234 site pairs from direct correlations between sites in concurrent and compensatory 235 substitutions within the same branches of a phylogenetic tree (Miyazawa 2013). 236 In this method, substitution probability and mean changes of physico-chemical 237 properties of side chain accompanied by amino acid substitutions at each site in 238 each branch of the tree are estimated with the likelihood of each substitution to 239 detect concurrent and compensatory substitutions. Then, partial correlation coefficients of the vectors of their characteristic changes accompanied by substitutions, 241 substitution probability and mean changes of physico-chemical properties, along 242 branches between sites are calculated to extract direct correlations in coevolutionary 243

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substitutions and employed as a score for residue-residue contact. The accuracy of 244 contact prediction by this method was comparable with that by mfDCA (Miyazawa 245 2013). This method, however, has a drawback to be computationally intensive, 246 because an optimum phylogenetic tree must be estimated. 247

9.3 Machine Learning Methods to Augment the Contact Prediction Accuracy Based on Amino Acid Coevolution

All the DCA methods such as mfDCA, plmDCA, GREMLIN, and PSICOV predict 250 significantly nonoverlapping sets of contacts (Jones et al. 2015; Kosciolek and Jones 251 2016; Wuyun et al. 2016). Then, increasing prediction accuracy by combining 252 their predictions together with other sequence/structure information have been 253 attempted (Skwark et al. 2013, 2014, 2016; Kosciolek and Jones 2014, 2016; Jones 254 et al. 2015; Wang et al. 2017; Shendure and Ji 2017); see Table 9.3.

PconsC (Skwark et al. 2013) combines the predictions of PSICOV and plmDCA 256 into a machine learning method, random forests, and employs alignments with 257 HHblits (Remmert et al. 2012) and jackHMMer (Johnson et al. 2010) at four 258 different e-value cut-offs. Five-layer neural network is employed instead of random 259 forests in PconsC2 (Skwark et al. 2014), and plmDCA and GaussDCA are employed 260 in PconsC3 (Skwark et al. 2016). A receptive field consisting of 11×11 predicted 261 contacts around each residue pair is taken into account in each layer except the first 262 one.

Name	Basic method	Post-processing	t9.1
PconsC3 (Skwark et al. 2016)	plmDCA, GaussDCA	5 layer DNN; http://c3.pcons.net. PconsC (Skwark et al. 2013), PconsC2 (Skwark et al. 2014)	t9.2
MetaPSICOV (Kosciolek and Jones 2014, 2016; Jones et al. 2015)	PSICOV, mfDCA, GREMLIN/CCMpred	A two stage neural network predictor; CONSIP2 pipeline http://bioinf.cs.ucl.ac.uk/MetaPSICOV	t9.3
RaptorX (Wang et al. 2017)	CCMpred	Ultra-deep learning model consisting of 1- and 2-dimensional convolutional residual neural networks http://raptorx.uchicago.edu/ContactMap/	t9.4
iFold (CASP12 2017)		Deep neural network (DNN)	t9.5
EPSILON-CP	PSICOV, GREMLIN, mfDCA, CCMpred, GaussDCA	4 hidden layer neural network with 400-200-200-50 neurons (Shendure and Ji 2017)	t9.6

 Table 9.3 Machine learning methods that combine predicted direct couplings with other sequence/structure information

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MetaPSICOV (Jones et al. 2015; Kosciolek and Jones 2016) combines the 264 predictions of PSICOV, mfDCA, and CCMpred/GREMLIN into the first stage of 265 a two-stage neural network predictor together with a well-established "classic" 266 machine learning contact predictor, which utilizes many features such as amino acid 267 profiles, predicted secondary structure and solvent accessibility along with sequence 268 separation predicted, as an additional source of information for a little depth of 269 MSAs. The second stage analyses the output of the first stage to eliminate outliers 270 and to fill in the gaps in the contact map. On a set of 40 target domains with a 271 median family size of around 40 effective sequences in CASPII, CONSIP2 server 272 achieved an average top-L/5 long-range contact precision of 27% (Kosciolek and 273 Jones 2016).

Wang et al. (2017) have also shown that a ultra-deep neural network (RaptorX) 275 can significantly improve contact prediction based on amino acid coevolution. They 276 have modeled short-range and long-range correlations in sequential and structural 277 features with respect to complex sequence-structure relationships in proteins by one-278 dimensional and two-dimensional deep neural networks (DNN), respectively. Both 279 the DNNs are convolutional residual neural networks. The 1D DNN performs convolutional transformations, with respect to residue position, of sequential features 281 such as position-dependent scoring matrix, predicted 3-state secondary structure and 3-state solvent accessibility. The 2D DNN does 2D convolutional transformations 283 of pairwise features such as coevolutional information calculated by CCMpred, 284 mutual information, pairwise contact potentials as well as the output of the 1D 285 DNN converted by a similar operation to outer product. Residual neural networks 286 are employed because they can pass both linear and nonlinear informations from 287 initial input to final output, making their training relatively easy. 288

9.4 Performance of Contact Prediction

New statistical methods based on the direct coupling analysis are confirmed in 290 various benchmarking studies (Moult et al. 2016; CASP12 2017; Kamisetty et al. 291 2013; Wuyun et al. 2016) to show remarkable accuracy of contact prediction, 292 although deep, stable alignments are required. They can more accurately detect 293 a higher number of contacts between residues, which are very distant along 294 sequence (Morcos et al. 2011). The top-scoring residue couplings are not only 295 sufficiently accurate but also well-distributed to define the 3D protein fold with 296 remarkable accuracy (Marks et al. 2011); this observation was quantified by 297 computing, from sequence alone, all-atom 3D structures of 15 test proteins from 298 different fold classes, ranging in size from 50 to 260 residues, including a G-protein 300 than on α proteins (Miyazawa 2013). These initial findings on a limited number of 301 proteins were confirmed as a general trend in a large-scale comparative assessment 302 of contact prediction methods (Wuyun et al. 2016; Adhikari et al. 2016).

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In CASP12, RaptorX performed the best in terms of F1 score for top L/2 longand medium-range contacts of 38 free-modeling (FM) targets; the total F1 score of RaptorX was better by about 7.6% and 10.0% than the second and third best servers, iFold_1 and the revised MetaPSICOV, respectively (Wang et al. 2017; 307 CASP12 2017). Tested on 105 CASP11 targets, 76 past CAMEO hard targets, and 398 membrane proteins, the average top L(L/10) long-range prediction accuracies of RaptorX are 0.47(0.77) in comparison with 0.30(0.59) for MetaPSICOV and 0.21(0.47) for CCMpred (Wang et al. 2017; CASP12 2017).

9.4.1 MSA Dependence of Contact Prediction Accuracy

In the direct-coupling-based methods, the accuracy of predicted contacts depends on the depth (Miyazawa 2013; Kamisetty et al. 2013; Wuyun et al. 2016) and quality of multiple sequence alignment (MSA) for a target. $5 \times L$ (protein length) aligned sequences may be desirable for accurate contact predictions (Kamisetty et al. 2013), although attempts to improve prediction methods for fewer aligned sequences have been made (Skwark et al. 2013, 2014, 2016; Wang et al. 2017). PconsC3 can be used for families with as little as 100 effective sequence members (Skwark et al. 2016). Also, RaptorX (Wang et al. 2017) attained top-L/2-accuracy >0.3 for long-rang contacts even by using MSAs with 20 effective sequence members.

Deepest MSAs including a target sequence were built with various values of 322 E-value cutoff (Skwark et al. 2013) and coverage parameters (Jones et al. 2015; 323 Kosciolek and Jones 2016) in sequence search and alignment programs based on 324 the hidden Markov models such as HHblits and jackHMMer. Although prediction 325 performance tends to increase in general as alignment depth is deeper (Miyazawa 326 2013), it was reported (Kosciolek and Jones 2016) that in the case of transmembrane 327 domains, building too deep alignments could result in unrelated sequences or 328 drifted domains being included. To increase alignment quality, E-value and coverage 329 parameters may be carefully tuned for each alignment (Kosciolek and Jones 330 2016). In the case of alignments that might contain regions of partial matches, 331 a too stringent sequence coverage requirement could result in missing related 332 sequences. On the other hand, a too permissive sequence coverage requirement 333 could pick up unrelated sequences, permitting many partial matches. A trade-off 334 is required between the effective number of sequences and sequence coverage, and 335 an appropriate E-value must be chosen not to much decrease both alignment depth 336 and sequence coverage (Hopf et al. 2012). 337

9.5 Contact-Guided de novo Protein Structure Prediction 338

It is a primary obstacle to de novo structure prediction that current methods and 339 computers cannot make it feasible to adequately sample the vast conformational 340

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space a protein might take in the precess of folding into the native structure (Kim 341 et al. 2009). Thus, it is critical whether residue-residue proximities inferred with 342 direct coupling analysis can provide sufficient information to reduce a huge search 343 space for a protein fold, without any known 3D structural information of the protein. 344

Algorithms are needed to fold proteins into native folds based on contact ³⁴⁵ information; see Table 9.4. Distance geometry generation (Havel et al. 1983; Braun ³⁴⁶ and Go 1985) of 3D structures, which may be followed by energy minimization and ³⁴⁷ molecular dynamics, will be just the primary one. In EVfold (Marks et al. 2011), ³⁴⁸ contacts inferred by direct coupling analysis and predicted secondary structure ³⁴⁹ information are translated into a set of distance constraints for the use of a distance ³⁵⁰ geometry algorithm in the Crystallography and NMR System (CNS) (Brünger ³⁵¹ 2007). It was confirmed that the evolutionary inferred contacts can sufficiently ³⁵² reduce a search space in the structure predictions of 15 test proteins from different ³⁵³ fold classes (Marks et al. 2011), and of 11 unknown and 23 known transmembrane ³⁵⁴ protein structures (Hopf et al. 2012). Because distance constraints from predicted ³⁵⁵ contacts may be partial in a protein sequence, they should be embedded into ab ³⁵⁶ initio structure prediction methods. ³⁵⁷

Name	Contact prediction	
EVfold (Marks et al. 2011, 2012)/EVfold_membrane (Hopf et al. 2012)	mfDCA/plmDCA	Using distance geometry algorithm (Havel et al. 1983) and simulated annealing of CNS (Brünger 2007); http://evfold.org/
DCA-fold (Sufkowska et al. 2012)	mfDCA	Simulated annealing using a coarse-grained molecular dynamics for a C_{α} model
FRAGFOLD/FILM3	MetaPSICOV	Combining fragment-based folding algorithm (Jones et al. 2005) with PSICOV (Kosciolek and Jones 2014) and with MetaPSICOV (Jones et al. 2015).
,40		FILM3 (Nugent and Jones 2012) is employed instead of FRAGFOLD (Jones 2001) for transmembrane proteins.
CONFOLD (Adhikari et al. 2015)	EVFOLD/FRAGFOLD (PSIPRED for 2nd structures)	Two-stage contact-guided de novo protein folding, using distance geometry simulated annealing protocol in a revised CNS v1.3.
		http://protein.rnet.missouri.edu/ confold/
Rosetta (Kim et al. 2004; Ovchinnikov et al. 2016)	GREMLIN	Fragment assembly

 Table 9.4
 Contact-guided de novo protein structure prediction methods and servers

Sulkowska et al. also showed that a simple hybrid method, called DCA-fold, 358 integrating mfDCA-predicted contacts with an accurate knowledge of secondary 359 structure is sufficient to fold proteins in the range of 1–3 Å resolution (Sufkowska 360 et al. 2012). In this study, simulated annealing using a coarse-grained molecular 361 dynamics model was employed for a C_{α} chain model, in which C_{α} s interact with 362 each other with a contact potential approximated by a Gaussian function and a 363 torsional potential depending on C_{α} dihedral angles at each position. 364

Adhikari et al. (2015) studied a way to effectively encode secondary structure 365 information into distance and dihedral angle constrains that complement long-range 366 contact constraints, and revised the CNS v1.3 to effectively use secondary structure 367 constraints together with predicted long-range constraints; CONFOLD (Adhikari 368 et al. 2015) consists of two stages. In the first stage secondary structure information 369 is converted into distance, dihedral angle, and hydrogen bond constraints, and then 370 best models are selected by executing the distance geometry simulated annealing. 371 In the second stage self-conflicting contacts in the best structure predicted in the 372 first stage are removed, constrains based on the secondary structures are refined, 373 and again the distance geometry simulated annealing is executed. 374

Baker group (Ovchinnikov et al. 2016) embedded contact constraints predicted 375 by GREMLIN (Kamisetty et al. 2013) as sigmoidal constraints to overcome noise 376 in the Rosetta (Kim et al. 2004) conformational sampling and refinement. They 377 found that model accuracy will be generally improved, if more than 3 L (protein 378 length) sequences are available, and that large topologically complex proteins can 379 be modeled with close to atomic-level accuracy without knowledge of homologous 380 structures, if there are enough homologous sequences available. 381

On the other hand, a fragment-based folding algorithm FRAGFOLD was combined with PSICOV (Kosciolek and Jones 2014) and with MetaPSICOV (Jones 383 et al. 2015; Kosciolek and Jones 2016); In this approach, predicted contacts are 384 converted into additional energy terms for FRAGFOLD in addition to the pairwise 385 potentials of mean force and solvation (Jones et al. 2015; Kosciolek and Jones 386 2016). FILM3 (Nugent and Jones 2012), with constraints based on predicted 387 contacts and ones approximating Z-coordinate values within the lipid membrane, 388 is employed instead of FRAGFOLD for transmembrane proteins. 389

RaptorX (Wang et al. 2017) employed the CNS suite (Brünger 2007) to generate 390 3D models from predicted contacts and secondary structure converted to distance, 391 angle and h-bond restraints, and could yield TMscore >0.6 for 203 of 579 test 392 proteins, while using MetaPSICOV and CCMpred could do so for 79 and 62, 393 respectively. 394

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9.5.1 How Many Predicted Contacts Should Be Used to Build **3D** Models?

The number of feasible contacts surrounding a residue in a protein is about 6.3 397 (Miyazawa and Jernigan 1996), which corresponds to the maximum number of 398 contacts per a protein, 6.3L/2, where L denotes protein length. However, more than 399 50% of known 3D structures in the PDB have less than 2L contacts, and in the test 400 on 15 proteins in EVfold benchmark set, less than 1.6L predicted contacts yielded 401 best results (Adhikari et al. 2015). In the original EVfold, the optimal number 402 of evolutionary constraints was in the order of 0.5L to 0.7L (Hopf et al. 2012). 403 Because prediction accuracy tends to decrease as the rank of contact score increases, 404 and different proteins need different numbers of predicted contacts to be folded 405 well, protein folds were generated with a wide range of the number of predicted 406 contacts, and then best folds were selected; from 30 to L in EVfold (Hopf et al. 4072012), and from 0.4L to 2.2L in CONFOLD (Adhikari et al. 2015). In RaptorX, the 408 top 2L predicted contacts irrespective of site separation were converted to distance 409 restraints (Wang et al. 2017). On the other hand, Jones group reported (Kosciolek 410 and Jones 2014) that artificially truncating the list of predicted contacts was likely 411 to remove useful information to fold a protein with FRAGFOLD and PSICOV, in 412 which the weight of a given predicted contact is determined by its positive predictive 413 value. 414

Evolutionary Direct Couplings Between Residues Not 9.6 415 **Contacting in a Protein 3D Structure** 416

Needless to say, evolutionary constraints do not only originate in intra-molecular 417 contacts but also result from inter-molecular contacts/interactions. Even in the case 418 of intra-molecular contacts, if there are structural variations including ones due to 419 conformational changes in a protein family, evolutionary constraints will reflect 420 the alternative conformations (Morcos et al. 2011; Hopf et al. 2012; Anishchenko 421 et al. 2013). Also, intra-molecular residue couplings may contain useful information 422 of ligand-mediated residue couplings (Morcos et al. 2011; Ovchinnikov et al. 423 2016). On the other hand, inter-molecular contacts may allow us to predict protein 424 complexes, and are useful to build protein-protein interaction networks at a residue 425 level. 426

9.6.1 Structural Variation Including Conformational Changes 427

MSA contains information on all members of the protein family, and direct 428 couplings between residues estimated from the MSA reflect the structures of all 429

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members. It was shown (Anishchenko et al. 2013) that 74% of top L/2 direct 430 couplings residue pairs that are more than 5 Å apart in the target structures of 3883 431 proteins are less than 5 Å apart in at least one homolog structure.

Conformational change is an interesting case of structural variation. Many pro- 433 teins adopt different conformations as part of their functions (Tokuriki and Tawfik 434 2009), indicating that protein flexibility is as important as structure on biological 435 function. Protein flexibility around the energy minimum can be studied by sampling 436 around the native structure in normal mode/principal component analysis, coarse- 437 grained elastic network model, and short-timescale MD simulations. However, 438 distant conformers that require large conformational transitions are difficult to 439 predict. If conformational changes are essential on protein functions, evolutionary 440 constraints will reflect the multiple conformations. Toth-Petroczy et al. (2016) 441 showed that coevolutionary information may reveal alternative structural states of 442 disorderd regions. 443

Morcos et al. (2011) found that some of top predicted contacts in the response- 444 regulator DNA-binding domain family (GerE, PF00196) conflict with the structure 445 (PDB ID 3C3W) of the full-length response-regulator DosR of M. tuberculosis, but 446 are compatible with the structure (PDB ID 1JE8) of DNA-binding domain of E. coli 447 NarL. 448

Sutto et al. (2015) combined coevolutionary data and molecular dynamics 449 simulations to study protein conformational heterogeneity; the Boltzmann-learning 450 algorithm with ℓ_2 regularization terms was employed to extract direct couplings 451 between sites in homologous protein sequences, and a set of conformations con- 452 sistent with the observed residue couplings were generated by exhaustive sampling 453 simulations based on a coarse-grained protein model. Although the most represen- 454 tative structure was consistent with the experimental fold, the various regions of the 455 sequence showed different stability, indicating conformational changes (Sutto et al. 456 2015). 457

Sfriso et al. (2016) made an automated pipeline based on discrete molecular 458 dynamics guided by predicted contacts for the systematic identification of functional 459 conformations in proteins, and identified alternative conformers in 70 of 92 proteins 460 in a validation set of proteins in PDB; various conformational transitions are relevant 461 to those conformers, such as open-closed, rotation, rotation-closed, concerted, and 462 miscellanea of complex motions. 463

Homo-Oligomer Contacts 9.6.2

Intra-molecular contacts that conflict with the native fold may indicate homo- 465 oligomer contacts (Anishchenko et al. 2013). Such a case was confirmed for 466 homo-oligomer contacts in the ATPase domain of nitrogen regulatory protein C- 467 like sigma-54 dependent transcriptional activators (Morcos et al. 2011) and between 468 transmembrane helices (Hopf et al. 2012). It was pointed out (Hopf et al. 2012) that 469

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the identification of evolutionary couplings due to homo-oligomerization is not only 470 meaningful in itself but also useful because their removal improves the accuracy of 471 the structure prediction for the monomer. 472

9.6.3 Residue Couplings Mediated by Binding to a Third Agent 473

Direct couplings between residues found by the DCA analysis can be medi- 474 ated (Morcos et al. 2011) by their interactions with a third agent, i.e., ligands, 475 substrates, RNA, DNA, and other metabolites. This indicates that binding sites with 476 such a agent may be found as residue sites directly coupled but not in contact.

If interactions with a third agent requires too specific residue type at a certain 478 site, then the residue type will be well conserved at the binding sites. This often 479 occurs, and has been utilized to identify binding sites. However, the interactions for 480 binding are less specific but certainly restricted, direct couplings between residues 481 around the binding sites may occurs. 482

Hopf et al. (2012) devised a total evolutionary coupling score, which is defined 483 as EC values summed over all high-ranking pairs involving a given residue and 484 normalized by their average over all high-ranking pairs, and showed that residues 485 with high total coupling scores line substrate-binding sites and affect signaling or 486 transport in transmembrane proteins, Adrb2 and Opsd. 487

9.7 Heterogeneous Protein-Protein Contacts

An application of the direct coupling analysis to predict the structures of protein 489 complexes is straightforward. In place of a MSA of a single protein family, a single 490 MSA that is built by concatenating the multiple MSAs of multiple protein families 491 every species can be employed to extract direct couplings between sites of different 492 proteins by removing indirect intra- and inter-protein couplings (Pazos et al. 1997; 493 Skerker et al. 2008; Weigt et al. 2009; Hopf et al. 2012). 494

A critical requirement for sequences to be concatenated is, however, that 495 respective sets of the protein sequences must have the same evolutionary history 496 to coevolve. In other words, phylogenetic trees built from the respective sets of 497 sequences employed for the protein families must have at least the same topology. 498 One way to build a set of cognate pairs of protein sequences is to employ 499 orthologous sequences for each protein family, the phylogenetic tree of which 500 coincides with that of species. Thus, a genome-wide analysis of finding protein-501 protein interactions based on protein sequences is not so simple.

Weigt et al. (2009) successfully applied the direct coupling analysis to the 503 bacterial two-component signal transduction system consisting of sensor kinase 504 (SK) and response regulator (RR), which are believed (Skerker et al. 2008) to 505 interact specifically with each other in most cases and often revealed by adjacency 506

in chromosomal location. This analysis is based on the fact that in prokaryotes 507 cognate pairs are often encoded in the same operon. Genome-sequencing projects 508 have revealed that most organisms contain large expansions of a relatively small 509 number of signaling families (Skerker et al. 2008). However, it is not as simple as in 510 prokaryotes to build a set of cognate pairs of those protein sequences in eukaryotes. 511

Hopf et al. (2014) developed a contact score, EVcomplex, for every interprotein residue pair based on the overall inter-protein EC score distributions, 513 evaluated its performance in blinded tests on 76 complexes of known 3D structure, 514 predicted protein-protein contacts in 32 complexes of unknown structure, and then 515 demonstrated how evolutionary direct couplings can be used to distinguish between 516 interacting and non-interacting protein pairs in a large complex. In their analysis, 517 protein sequence pairs that are encoded close on *E. coli* genome were employed to 518 reduce incorrect protein pairings. 519

9.8 Discussion

Determination of protein structure is essential to understand protein function. ⁵²¹ However, despite significant effort to explore unknown folds in the protein structural ⁵²² space, protein structures determined by experiment are far less than known protein ⁵²³ families. Only about 41–42% of the Pfam families (Finn et al. 2016) (Pfam-⁵²⁴ A release 31.0, 16712 families) include at least one member whose structure is ⁵²⁵ known. The number and also the size of protein families will further grow as ⁵²⁶ genome/metagenome sequencing projects proceed with next-generation sequencing ⁵²⁷ technologies. Thus, accurate de novo prediction of three-dimensional structure is ⁵²⁸ desirable to catch up with the high growing speed of protein families with unknown ⁵²⁹ folds. Coevolutionary information can be used to predict not only proteins but ⁵³⁰ also RNAs (Weinreb et al. 2016) and those complexes, together with experimental ⁵³¹ informations such as X-ray, NMR, SAS, FRET, crosslinking, Cryo-EM, and others. ⁵³²

Here, statistical methods for disentangling direct from indirect couplings 533 between sites with respect to evolutionary variations/substitutions of amino acids 534 in homologous proteins have been briefly reviewed. Dramatic improvements on 535 contact prediction and successful 3D de novo predictions based on predicted 536 contacts are described in details in the recent reports of CASP-11 (Moult et al. 2016) 537 and CASP-12 meetings (CASP12 2017). Machine learning methods, particularly 538 deep neural network (DNN) such as MetaPSICOV, iFold, and RaptorX, have 539 shown to significantly augment contact prediction accuracy based on coevolutionary 540 information. However, the present state-of-the-art DNN methods are, at least at the 541 very moment, not powerful enough to extract coevolutionary information directly 542 from homologous sequences. It was reported that without coevolutionary strength 543 produced by CCMpred the top L/10 long-range prediction accuracy of RaptorX 544 might drop by 0.15 for soluble proteins and more for membrane proteins (Wang 545 et al. 2017), indicating that the direct coupling analysis is still essential for contact 546 prediction. 547

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The primary requirement for the direct coupling analysis is a high quality 548 deep alignment. However, genome/metagenome sequencing projects provide more 549 genetic variations from which more accurate and more comprehensive information 550 on evolutionary constraints can be extracted. One of problems is that species being 551 sequenced may be strongly biased to prokaryotes, making it hard to analyze eukary-552 otic proteins based on coevolutionary substitutions. Experiments of vitro evolution 553 may be useful to provide sequence variations for eukaryotic proteins (Ovchinnikov 554 et al. 2016).

For a large-scale of protein structure prediction, computationally intensive methods such as the ACE and Boltzmann machine (MCMC and mpDCA) can hardly be employed. The Gaussian approximation with a normal-inverse-Wishart prior, the Gaussian approximations with other priors (PSICOV) and mean field approximation (mfDCA) are fast enough but their performance of contact prediction tends to be compared unfavorably with the pseudo-likelihood approximation (plmDCA), indicating that they may be inappropriate for proteins with sparse couplings.

The accurate estimates of fields and couplings are very informative in evaluating 563 the effects (ΔH_{Potts}) of mutations (Hopf et al. 2017), identifying protein family 564 members and also studying folding mechanisms (Morcos et al. 2014; Jacquin et al. 565 2016) and protein evolution (Miyazawa 2017b). It should be also examined whether 566 the distribution of dimensionless energies (H_{Potts}) over homologous proteins can be 567 well reproduced. Accuracy of estimates of fields and couplings and the distribution 568 of dimensionless energies depends on regularization parameters or the ratio of 569 pseudocount (Barton et al. 2016; Miyazawa 2017b), and therefore they should be 570 optimized. It was also pointed out that group L_1 regularization performs better 571 than L_2 for the maximum pseudolikelihood method (Ingraham and Marks 2016). 572 The ACE algorithm, which can be applied only for systems of sparse couplings, 573 may be moer favorable with respect to computational load for the estimation of 574 fields and couplings than Boltzmann learning with Monte Carlo simulation or 575 with message passing. However, both the methods are computationally intensive. 576 Recently, another approach consisting of two methods named persistent-vi and 577 Fadeout, in which the posterior probability density with horseshoe prior is approx-578 imately estimated by using variational inference and noncentered parameterization 579 for such a sparsity-inducing prior, has shown to perform better with twofold 580 cpu time than the maximum pseudolikelihood method with L_2 and group L_1 581 regularizations (Ingraham and Marks 2016). 582

The remarkable advances of sequencing technologies and also statistical methods 583 are likely to bring many targets within range of the present approach in the near 584 future, and have a potential to transform the field (Moult et al. 2016). 585

Appendix

An appendix described in full will be found in the article (Miyazawa 2017a) 587 submitted to the arXiv. 588

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Inverse Potts Model

A Gauge Employed for $h_i(a_k)$ and $J_{ii}(a_k, a_l)$

Unless specified, a following gauge is employed; we call it q-gauge, here.

$$h_i(a_q) = J_{ij}(a_k, a_q) = J_{ij}(a_q, a_l) = 0$$
 (9.16)

In this gauge, the amino acid a_q is the reference state for fields and couplings, 592 and $P_i(a_q)$, $P_{ij}(a_k, a_q) = P_{ji}(a_q, a_k)$, and $P_{ij}(a_q, a_q)$ are regarded as dependent 593 variables. Common choices for the reference state a_q are the most common 594 (consensus) state at each site. Any gauge can be transformed to another by the 595 following transformation. 596

$$J_{ij}^{I}(a_{k}, a_{l}) \equiv J_{ij}(a_{k}, a_{l}) - J_{ij}(\cdot, a_{l}) - J_{ij}(a_{k}, \cdot) + J_{ij}(\cdot, \cdot)$$
(9.17)

$$h_{i}^{I}(a_{k}) \equiv h_{i}(a_{k}) - h_{i}(\cdot) + \sum_{j \neq i} (J_{ij}(a_{k}, \cdot) - J_{ij}(\cdot, \cdot))$$
(9.18)

where "." denotes the reference state, which may be a_a for each site (q-gauge) or 597 the average over all states (Ising gauge). 598

Boltzmann Machine

Fields $h_i(a_k)$ and couplings $J_{ij}(a_k, a_l)$ are estimated by iterating the following 2- 600 step procedures. 601

- 1. For a given set of h_i and $J_{ij}(a_k, a_l)$, marginal probabilities, $P^{\text{MC}}(\mathbf{g}_i = a_k)$ 602 and $P^{MC}(\mathbf{\sigma}_i = a_k, \mathbf{\sigma}_i = a_l)$, are estimated by a Markov chain Monte Carlo 603 method (the Metropolis-Hastings algorithm (Metropolis et al. 1953)) or by any 604 other method (for example, the message passing algorithm (Weigt et al. 2009)). 605
- 2. Then, h_i and $J_{ij}(a_k, a_l)$ are updated according to the gradient of negative log- 606 posterior-probability per instance, $\partial S_0/\partial h_i(a_k)$ or $\partial S_0/\partial J_{ii}(a_k, a_l)$, multiplied 607 by a parameter-specific weight factor (Barton et al. 2016), $w_i(a_k)$ or $w_{ii}(a_k, a_l)$; 608 see Eqs. 9.8 and 9.12. 609

$$\Delta h_i(a_k) = -(P^{\mathrm{MC}}(\mathbf{g}_i = a_k) + \frac{\partial R}{\partial h_i(a_k)} - P_i(a_k)) \cdot w_i(a_k)$$
(9.19)
$$\Delta J_{ij}(a_k, a_l) = -(P^{\mathrm{MC}}(\mathbf{g}_i = a_k, \mathbf{g}_i = a_l) + \frac{\partial R}{\partial J_{ij}(a_k, a_l)}$$

$$-P_{ij}(a_k, a_l)) \cdot w_{ij}(a_k, a_l) \tag{9.20}$$

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where weights are also updated as $w_i(a_k) \leftarrow f(w_i(a_k))$ and $w_{ij}(a_k, a_l) \leftarrow 611$ $f(w_{ij}(a_k, a_l))$ according to the RPROP (Riedmiller and Braun 1993) algorithm; 612 the function f(w) is defined as 613

$$f(w) \equiv \begin{cases} \max(w \cdot s_{-}, w_{\min}) \text{ if the gradient changes its sign,} \\ \min(w \cdot s_{+}, w_{\max}) \text{ otherwise} \end{cases}$$
(9.21)

 $w_{\min} = 10^{-3}$, $w_{\max} = 10$, $s_{-} = 0.5$, and $s_{+} = 1.9 < 1/s_{-}$ were 614 employed (Barton et al. 2016). After updated, $h_i(a_k)$ and $J_{ij}(a_k, a_l)$ may be 615 modified to satisfy a given gauge.

The Boltzmann machine has a merit that model correlations are calculated.

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Gaussian Approximation for $P(\sigma)$ with a Normal-Inverse-Wishart Prior

The normal-inverse-Wishart distribution (NIW) is the product of the multivariate ⁶¹⁹ normal distribution (\mathcal{N}) and the inverse-Wishart distribution (\mathcal{W}^{-1}), which are ⁶²⁰ the conjugate priors for the mean vector and for the covariance matrix of a ⁶²¹ multivariate Gaussian distribution, respectively. The NIW is employed as a prior ⁶²² in GaussDCA (Baldassi et al. 2014), in which the sequence distribution $P(\sigma)$ ⁶²³ is approximated as a Gaussian distribution. In this approximation, the q-gauge ⁶²⁴ is used, and $P_i(a_q)$, $P_{ij}(a_k, a_q) = P_{ji}(a_q, a_k)$, and $P_{ij}(a_q, a_q)$ are regarded as ⁶²⁵ dependent variables; see section "A Gauge Employed for $h_i(a_k)$ and $J_{ij}(a_k, a_l)$ "; in ⁶²⁶ GaussDCA, deletion is excluded from independent variables.

The posterior distribution for the NIW is also a NIW. Thus, the cross entropy S_0 628 can be represented as 629

$$S_{0}(\boldsymbol{\mu}, \boldsymbol{\Sigma}|\{P_{i}\}, \{P_{ij}\}) = \frac{-1}{B} \log[\prod_{\tau=1}^{B} \mathcal{N}(\{\delta_{\boldsymbol{\theta}_{i}^{\tau}a_{k}}\}|\boldsymbol{\mu}, \boldsymbol{\Sigma})\mathcal{N}(\boldsymbol{\mu}|\boldsymbol{\mu}^{0}, \boldsymbol{\Sigma}/\kappa)\mathcal{W}^{-1}(\boldsymbol{\Sigma}|\boldsymbol{\Lambda}, \boldsymbol{v})]$$
(9.22)

$$= \frac{-1}{B} \log[\mathcal{N}(\boldsymbol{\mu}|\boldsymbol{\mu}^{B}, \boldsymbol{\Sigma}/\boldsymbol{\kappa}^{B}) \mathcal{W}^{-1}(\boldsymbol{\Sigma}|\boldsymbol{\Lambda}^{B}, \boldsymbol{v}^{B})$$
(9.23)

$$(\det(2\pi\Sigma))^{-B/2} \left(\frac{\kappa}{\kappa^B}\right)^{\dim\Sigma/2} \frac{(\det(\Lambda/2))^{\nu/2}}{(\det(\Lambda^B/2))^{\nu^B/2}} \frac{\Gamma_{\dim\Sigma}(\nu^B/2)}{\Gamma_{\dim\Sigma}(\nu/2)} (\det\Sigma)^{-(\nu-\nu^B)^2}]$$
(9.24)

where $\Gamma_{\dim \Sigma}(v/2)$ is the multivariate Γ function, μ is the mean vector, and dim Σ ⁶³⁰ is the dimension of covariance matrix Σ , dim $\Sigma = (q - 1)L$ excluding deletion in ⁶³¹ GaussDCA. The normal and NIW distributions are defined as follows. ⁶³²

$$\mathcal{N}(\boldsymbol{\mu}|\boldsymbol{\mu}^{0}, \Sigma) \equiv (\det(2\pi\Sigma))^{-1/2} \exp(-\frac{(\boldsymbol{\mu}-\boldsymbol{\mu}^{0})^{T}\Sigma^{-1}(\boldsymbol{\mu}-\boldsymbol{\mu}^{0})}{2})$$
(9.25)

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$$\mathcal{W}^{-1}(\Sigma|\Lambda, v) \equiv \frac{(\det(\Lambda/2))^{v/2}}{\Gamma_{\dim\Sigma}(v/2)} (\det\Sigma)^{-(v+\dim\Sigma+1)/2} \exp(-\frac{1}{2} \operatorname{Tr}\Lambda\Sigma^{-1}) \quad (9.26)$$

Parameters μ^B , κ^B , v^B , and Λ^B satisfy

-

$$\mathbf{P}_{i}^{B}(a_{k}) = (\kappa \mathbf{P}_{i}^{0}(a_{k}) + BP_{i}(a_{k}))/(\kappa + B), \ \kappa^{B} = \kappa + B, \ v^{B} = v + B$$
(9.27)

$$\Lambda_{ij}^{B}(a_{k}, a_{l}) = \Lambda_{ij}(a_{k}, a_{l}) + BC_{ij}(a_{k}, a_{l}) + \frac{\kappa B}{\kappa + B} [(P_{i}(a_{k}) - \mathbf{\mu}_{i}^{0}(a_{k}))(P_{j}(a_{l}) - \mathbf{\mu}_{j}^{0}(a_{l}))]$$
(9.28)

where the Λ and v are the scale matrix and the degree of freedom, respectively, 634 shaping the inverse-Wishart distribution, and *C* is the given covariance matrix; 635 $C_{ij}(a_k, a_l) \equiv P_{ij}(a_k, a_l) - P_i(a_k)P_i(a_l)$. The mean values of μ and Σ under NW 636 posterior are μ^B and $\Lambda^B/(v^B - \dim \Sigma - 1)$, and their mode values are μ^B and 637 $\Lambda^B/(v^B + \dim \Sigma + 1)$, which minimize the cross entropy or maximize the posterior 638 probability. The covariance matrix Σ can be estimated to be the exactly same value 639 by adjusting the value of v, whichever the mean posterior or the maximum posterior 640 is employed for the estimation of Σ . In GaussDCA, the mean posterior estimate 641 was employed but here the maximum posterior estimate is employed according to 642 the present formalism. 643

$$(\boldsymbol{\mu}, \Sigma) = \arg \min_{(\boldsymbol{\mu}, \Sigma)} S_0(\boldsymbol{\mu}, \Sigma | \{ P_i \}, \{ P_{ij} \}) = (\boldsymbol{\mu}^B, \Lambda^B / (v^B + \dim \Sigma + 1)) \quad (9.29)$$

According to GaussDCA, v is chosen in such a way that $\sum_{ij}(a_k, a_l)$ is nearly 644 equal to the covariance matrix corrected by pseudocount; $v = \kappa + \dim \Sigma + 1$ for the 645 mean posterior estimate in GaussDCA, but $v = \kappa - \dim \Sigma - 1$ for the maximum 646 posterior estimate here. 647

From Eq. 9.15, the estimates of couplings and fields are calculated.

$$J_{ij}^{\text{NIW}}(a_k, a_l) = -\frac{\partial S_0(\{P_i\}, \{P_{ij}\})}{\partial P_{ij}(a_k, a_l)} = -\frac{(\kappa + B + 1)}{\kappa + B} (\Sigma^{-1})_{ij}(a_k, a_l)$$
(9.30)

Because the number of instances is far greater than 1 ($B \gg 1$), these estimates of 649 couplings are practically equal to the estimates ($J^{\text{MF}} = -\Sigma^{-1}$) in the mean field 650 approximation, which was employed in GaussDCA (Baldassi et al. 2014). 651

$$h_{i}^{\text{NIW}}(a_{k}) = -\sum_{j \neq i} \sum_{l} J_{ij}^{\text{NIW}}(a_{k}, a_{l}) P_{j}(a_{l}) - \frac{(\kappa + B + 1)}{\kappa + B} \sum_{j} \sum_{l \neq q} (\Sigma^{-1})_{ij}(a_{k}, a_{l})$$
$$[\delta_{ij} \frac{\delta_{kl} - 2P_{i}(a_{l})}{2} + \frac{\kappa B}{\kappa + B} (P_{j}(a_{l}) - \mu_{j}^{0}(a_{l}))]$$
(9.31)

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The $(h_i^{\text{NIW}}(a_k) - h_i^{\text{NIW}}(a_q))$ does not converge to $\log P_i(a_k)/P_i(a_q)$ as $J^{\text{NIW}} \to 0$ 652 but $h_i^{\text{MF}}(a_k) - h_i^{\text{MF}}(a_q)$ does; in other words, the mean field approximation gives 653 a better *h* for the limiting case of no couplings than the present approximation. 654 Barton et al. (2016) reported that the Gaussian approximation generally gave a better 655 generative model than the mean field approximation. 656

In GaussDCA (Baldassi et al. 2014), μ^0 and Λ/κ were chosen to be as 657 uninformative as possible, i.e., mean and covariance for a uniform distribution. 658

$$\boldsymbol{\mu}_{i}^{0}(a_{k}) = 1/q, \quad \frac{\Lambda_{ij}(a_{k}, a_{l})}{\kappa} = \frac{\delta_{ij}}{q}(\delta_{kl} - \frac{1}{q}) \tag{9.32}$$

Pseudo-likelihood Approximation

Symmetric Pseudo-likelihood Maximization

The probability of an instance σ^{τ} is approximated as follows by the product of 661 conditional probabilities of observing $\hat{\sigma}_{i}^{\tau}$ under the given observations $\hat{\sigma}_{j\neq i}^{\tau}$ of all 662 other sites.

$$P(\mathbf{\sigma}^{\tau}) \approx \prod_{i} P(\mathbf{\sigma}_{i} = \mathbf{\sigma}_{i}^{\tau} | \{ \mathbf{\sigma}_{j \neq i} = \mathbf{\sigma}_{j}^{\tau} \})$$
(9.33)

Then, cross entropy is approximated as

$$S_0(h, J|\{P_i\}, \{P_{ij}\}) \approx S_0^{\text{PLM}}(h, J|\{P_i\}, \{P_{ij}\}) \equiv \sum_i S_{0,i}(h, J|\{P_i\}, \{P_{ij}\})$$
(9.34)

$$S_{0,i}(h, J|\{P_i\}, \{P_{ij}\}) \equiv \frac{-1}{B} \sum_{\tau} \ell_i (\mathbf{g}_i = \mathbf{g}_i^{\tau}|\{\mathbf{g}_{j\neq i} = \mathbf{g}_j^{\tau}\}, h, J) + R_i(h, J)$$
(9.35)

where conditional log-likelihoods and ℓ_2 norm regularization terms employed in $_{665}$ Ekeberg et al. (2013) are $_{666}$

$$\ell_{i}(\mathbf{g}_{i} = \mathbf{g}_{i}^{\tau} | \{ \mathbf{g}_{j\neq i} = \mathbf{g}_{j}^{\tau} \}, h, J) = \log\left[\frac{\exp(h_{i}(\mathbf{g}_{i}^{\tau}) + \sum_{j\neq i} J_{ij}(\mathbf{g}_{i}^{\tau}, \mathbf{g}_{j}^{\tau}))}{\sum_{k} \exp(h_{i}(a_{k}) + \sum_{j\neq i} J_{ij}(a_{k}, \mathbf{g}_{j}^{\tau}))}\right]$$

$$(9.36)$$

$$R_{i}(h, J) \equiv \gamma_{h} \sum_{k} h_{i}(a_{k})^{2} + \frac{\gamma_{J}}{2} \sum_{k} \sum_{j \neq i} \sum_{l} J_{ij}(a_{k}, a_{l})^{2}$$
(9.37)

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The optimum fields and couplings in this approximation are estimated by minimizing the pseudo-cross-entropy, S_0^{PLM} .

$$(h^{\text{PLM}}, J^{\text{PLM}}) = \arg\min_{h, J} S_0^{\text{PLM}}(h, J | \{P_i\}, \{P_{ij}\})$$
(9.38)

Equation 9.38 is not invariant under gauge transformation; the ℓ_2 norm reg- 670 ularization terms in Eq. 9.38 favors only a specific gauge that corresponds to 671 $\gamma_J \sum_l J_{ij}(a_k, a_l) = \gamma_h h_i(a_k), \gamma_J \sum_k J_{ij}(a_k, a_l) = \gamma_h h_j(a_l), \text{ and } \sum_k h_i(a_k) = 0$ 672 for all i, j(>i), k and l (Ekeberg et al. 2013). $\gamma_J = \gamma_h = 0.01$ that is relatively 673 a large value independent of B was employed in Ekeberg et al. (2013). $\gamma_h = 0.01$ 674 but $\gamma_J = q(L-1)\gamma_h$ were employed in Hopf et al. (2017), in which gapped sites 675 in each sequence were excluded in the calculation of the Hamiltonian $H(\sigma)$, and 676 therefore q = 20.

GREMLIN (Kamisetty et al. 2013) employs Gaussian prior probabilities that 678 depend on site pairs.

$$R_{i}(h, J) \equiv \gamma_{h} \sum_{k} h_{i}(a_{k})^{2} + \sum_{k} \sum_{j \neq i} \frac{\gamma_{ij}}{2} \sum_{l} J_{ij}(a_{k}, a_{l})^{2}$$
(9.39)

$$\gamma_{ij} \equiv \gamma_c (1 - \gamma_p \log(P_{ij}^0)) \tag{9.40}$$

where P_{ij}^0 is the prior probability of site pair (i, j) being in contact.

Asymmetric Pseudo-likelihood Maximization

To speed up the minimization of S_0 , a further approximation, in which $S_{0,i}$ is 682 separately minimized, is employed (Ekeberg et al. 2014), and fields and couplings 683 are estimated as follows. 684

$$J_{ij}^{\text{PLM}}(a_k, a_l) \simeq \frac{1}{2} (J_{ij}^*(a_k, a_l) + J_{ji}^*(a_l, a_k))$$
(9.41)

$$(h_i^{\text{PLM}}, J_i^*) = \arg\min_{h_i, J_i} S_{0,i}(h, J | \{P_i\}, \{P_{ij}\})$$
(9.42)

It is appropriate to transform h and J estimated above into a some specific gauge 685 such as the Ising gauge. 686

ACE (Adaptive Cluster Expansion) of Cross-Entropy for Sparse Markov Random Field 688

The cross entropy $S_0(\{h_i, J_{ij}\}|\{P_i\}, \{P_{ij}\}, i, j \in \Gamma)$ of a cluster of sites Γ , which 669 is defined as the negative log-likelihood per instance in Eq. 9.14, is approximately 690 minimized by taking account of sets $L_k(t)$ of only significant clusters consisting of 691

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k sites, the incremental entropy (cluster cross entropy) ΔS_{Γ} of which is significant 692 ($|\Delta S_{\Gamma}| > t$) (Cocco and Monasson 2011, 2012; Barton et al. 2016). 693

$$S_{0}(\{P_{i}, P_{ij} | i, j \in \Gamma\}) \simeq \sum_{l=1}^{|\Gamma|}, \sum_{\Gamma' \in L_{l}(t), \Gamma' \subset \Gamma} \Delta S_{0}(\{P_{i}, P_{ij} | i, j \in \Gamma'\})$$
(9.43)

$$\Delta S_0(\{P_i, P_{ij} | i, j \in \Gamma\}) \equiv S_0(\{P_i, P_{ij} | i, j \in \Gamma\}) - \sum_{\Gamma' \subset \Gamma} \Delta S_0(\{P_i, P_{ij} | i, j \in \Gamma'\})$$
(9.44)

$$= \sum_{\Gamma' \subseteq \Gamma} (-1)|\Gamma| - |\Gamma'| \ S_0(\{P_i, P_{ij} | i, j \in \Gamma'\})$$
(9.45)

 $L_{k+1}(t)$ is constructed from $L_k(t)$ by adding a cluster Γ consisting of (k+1) sites in 694 a lax case provided that any pair of size k clusters Γ^1 , $\Gamma^2 \in L_k(t)$ and $\Gamma^1 \cup \Gamma^2 = \Gamma$ 695 or in a strict case if $\Gamma' \in L_k(t)$ for $\forall \Gamma'$ such that $\Gamma' \subset \Gamma$ and $|\Gamma'| = k$. Thus, 696 Eq. 9.43 yields sparse solutions. The cross entropies $S_0(\{P_i, P_{ij} | i, j \in \Gamma'\})$ for the 697 small size of clusters are estimated by minimizing $S_0(\{h_i, J_{ij}\} | \{P_i, P_{ij}\}, i, j \in \Gamma')$ 698 with respect to fields and couplings. Starting from a large value of the threshold t 699 (typically t = 1), the cross-entropy $S_0(\{P_i, P_{ij}\} | i, j \in \{1, ..., N\})$ is calculated 700 by gradually decreasing t until its value converges. Convergence of the algorithm 701 may also be more difficult for alignments of long proteins or those with very strong 702 interactions. In such cases, strong regularization may be employed. 703

The following regularization terms of ℓ_2 norm are employed in ACE (Barton 704 et al. 2016), and so Eq. 9.43 is not invariant under gauge transformation. 705

$$-\frac{1}{B}\log P_0(h, J|i, j \in \Gamma) = \gamma_h \sum_{i \in \Gamma} \sum_k h_i (a_k)^2 + \gamma_J \sum_{i \in \Gamma} \sum_k \sum_{J>i, j \in \Gamma} \sum_l J_{ij} (a_k, a_l)^2$$
(9.46)

 $\gamma_h = \gamma_J \propto 1/B$ was employed (Barton et al. 2016).

The compression of the number of Potts states, $q_i \leq q$, at each site can be 707 taken into account. All infrequently observed states or states that insignificantly 708 contribute to site entropy can be treated as the same state, and a complete model can 709 be recovered (Barton et al. 2016) by setting $h_i(a_k) = h_i(a_{k'}) + \log(P_i(a_k)/P'_i(a_{k'}))$, 710 and $J_{ij}(a_k, a_l) = J'_{ij}(a_{k'}, a_{l'})$, where "j" denotes a corresponding aggregated state 711 and a potential.

Starting from the output set of the fields $h_i(a_k)$ and couplings $J_{ij}(a_k, a_l)$ obtained 713 from the cluster expansion of the cross-entropy, a Boltzmann machine is trained 714 with $P_i(a_k)$ and $P_{ij}(a_k)$ by the RPROP algorithm (Riedmiller and Braun 1993) 715 to refine the parameter values of h_i and $J_{ij}(a_k, a_l)$ (Barton et al. 2016); see 716 section "Boltzmann Machine". This post-processing is also useful because model 717 correlations are calculated.

An appropriate value of the regularization parameter for trypsin inhibitor were 719 much larger ($\gamma = 1$) for contact prediction than those ($\gamma = 2/B = 10^{-3}$) for 720



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recovering true fields and couplings (Barton et al. 2016), probably because the task 721

of contact prediction requires the relative ranking of interactions rather than their 722 actual values. 723

Scoring Methods for Contact Prediction

Corrected Frobenius Norm (L_{22} Matrix Norm), S_{ii}^{CFN}

For scoring, plmDCA (Ekeberg et al. 2013, 2014) employs the corrected Frobenius 726 norm of J_{ij}^{I} transformed in the Ising gauge, in which J_{ij}^{I} does not contain anything 727 that could have been explained by fields h_i and h_j ; $J_{ij}^{I}(a_k, a_l) \equiv J_{ij}(a_k, a_l) - 728$ $J_{ij}(\cdot, a_l) - J_{ij}(a_k, \cdot) + J_{ij}(\cdot, \cdot)$ where $J_{ij}(\cdot, a_l) = J_{ji}(a_l, \cdot) \equiv \sum_{k=1}^{q} J_{ij}(a_k, a_l)/q$. 729

$$\mathcal{S}_{ij}^{\text{CFN}} \equiv \mathcal{S}_{ij}^{\text{FN}} - \mathcal{S}_{.j}^{\text{FN}} \mathcal{S}_{i.}^{\text{FN}} / \mathcal{S}_{..}^{\text{FN}}, \quad \mathcal{S}_{ij}^{\text{FN}} \equiv \sqrt{\sum_{\kappa \neq \text{gap}} \sum_{l \neq \text{gap}} J_{ij}^1(a_k, a_l)^2}$$
(9.47)

where "·" denotes average over the indicated variable. This CFN score with the gap 730 state excluded in Eq. 9.47 performs better (Ekeberg et al. 2014; Baldassi et al. 2014) 731 than both scores of FN and DI/EC (Weigt et al. 2009; Morcos et al. 2011; Marks 732 et al. 2011; Hopf et al. 2012). 733

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