## Errata

for

"Prediction of contact residue pairs based on co-substitution between sites in protein structures", PLoS One, 8, e54252, 2013, doi:10.1371/journal.pone.0054252

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1. Eqs. 3 and 4 on page 2,

$$P(\mathcal{A}_i|T,\Theta,\theta_\alpha) = \sum_{\kappa} \sum_{\lambda} P(\mathcal{A}_i|v_{bL} = \kappa, v_{bR} = \lambda, T,\Theta,\theta_\alpha)$$
(3)

$$P(\mathcal{A}_{i}|v_{bL} = \kappa, v_{bR} = \lambda, T, \Theta, \theta_{\alpha}) \equiv P_{bL}(\mathcal{A}_{i}|v_{bL} = \kappa, T, \Theta, \theta_{\alpha}) f_{\kappa} P(\lambda|\kappa, t_{b}, \Theta, \theta_{\alpha}) P_{bR}(\mathcal{A}_{i}|v_{bR} = \lambda, T, \Theta, \theta_{\alpha})$$
(4)

and Eq. 6 on page 3,

$$\Delta_{ib}(\mathcal{A}_i, \hat{T}, \hat{\Theta}, \theta_\alpha) \equiv \sum_{\kappa, \lambda} \frac{\Delta_{\kappa, \lambda} P(\mathcal{A}_i | v_{bL} = \kappa, v_{bR} = \lambda, \hat{T}, \hat{\Theta}, \theta_\alpha)}{P(\mathcal{A}_i | \hat{T}, \hat{\Theta}, \theta_\alpha)}$$
(6)

should be

$$P(\mathcal{A}_i | T, \Theta, \theta_\alpha) = \sum_{\kappa} \sum_{\lambda} P(\mathcal{A}_i, v_{bL} = \kappa, v_{bR} = \lambda \mid T, \Theta, \theta_\alpha)$$
(3)

$$P(\mathcal{A}_{i}, v_{bL} = \kappa, v_{bR} = \lambda \mid T, \Theta, \theta_{\alpha}) = P_{bL}(\mathcal{A}_{i} \mid v_{bL} = \kappa, T, \Theta, \theta_{\alpha}) f_{\kappa} P(\lambda \mid \kappa, t_{b}, \Theta, \theta_{\alpha}) P_{bR}(\mathcal{A}_{i} \mid v_{bR} = \lambda, T, \Theta, \theta_{\alpha})$$
(4)

and

$$\Delta_{ib}(\mathcal{A}_i, \hat{T}, \hat{\Theta}, \theta_\alpha) \equiv \sum_{\kappa, \lambda} \frac{\Delta_{\kappa, \lambda} P(\mathcal{A}_i, v_{bL} = \kappa, v_{bR} = \lambda \mid \hat{T}, \hat{\Theta}, \theta_\alpha)}{P(\mathcal{A}_i \mid \hat{T}, \hat{\Theta}, \theta_\alpha)}$$
(6)

2. Figure 1 should be replaced by the figure shown on the next page; the edge of the lefthand side in the original is too much trimmed by one character.

**Topology:** Pfam reference tree

Branch lengths: by a ML method in a mechanistic codon substitution model



Correlation coefficient matrix of feature vectors between sites:

$$C_{ij} \equiv r_{\Delta_i \Delta_j} = \frac{(\boldsymbol{\Delta}_i, \boldsymbol{\Delta}_j)}{\|\boldsymbol{\Delta}_i\| \|\boldsymbol{\Delta}_j\|}$$

Partial correlation coefficients of feature vectors between sites:

$$\mathcal{C}_{ij} \equiv \frac{(\Pi_{\perp\{\Delta_{k\neq i,j}\}} \Delta_i, \Pi_{\perp\{\Delta_{k\neq i,j}\}} \Delta_j)}{\|\Pi_{\perp\{\Delta_{k\neq i,j}\}} \Delta_i\| \|\Pi_{\perp\{\Delta_{k\neq i,j}\}} \Delta_j\|} = -\frac{(C^{-1})_{ij}}{((C^{-1})_{ii}(C^{-1})_{jj})^{1/2}}$$

Co-evolution score based on partial correlation coefficients:

$$\begin{split} \rho_{ij} &\equiv \max[\rho_{ij}^{s}, \max(-\rho_{ij}^{v}, 0), \max(-\rho_{ij}^{c}, 0), \max(-\rho_{ij}^{hb}, 0), |\rho_{ij}^{h}|, \dots] \\ \rho_{ij}^{s} &\equiv \max(\mathcal{C}_{ij}^{s}, 0), \rho_{ij}^{x} \equiv \operatorname{sgn} \mathcal{C}_{ij}^{x} (|\rho_{ij}^{s} \mathcal{C}_{ij}^{x}|)^{1/2} \quad (x \in \{v, c, hb, h, \dots\}) \end{split}$$